

Statistics

Lecture 12



Feb 19-8:47 AM

I surveyed 275 students and 42% of them ^{SG 21}
 were in favor of multiple-choice exams.
 $n = 275$
 $\hat{p} = .42$
 $x = n\hat{p} = 275(.42) = 115.5 \rightarrow \boxed{x = 116}$
 if decimal $\rightarrow$ Round-up
 Find 98% Confidence interval for the proportion
 of all students that like multiple-choice exams.
 C-level: .98
 $\hat{p} - E < p < \hat{p} + E$
 1-Prop Z Int
 $x = 116$
 $n = 275$
 C-level: .98
 Calculate
 $E = \frac{.49 - .35}{2} = \boxed{.07}$
 $\hat{p} = \frac{.49 + .35}{2} = \boxed{.42}$

$\boxed{.35 < p < .49}$
 we are 98% Confident
 that between 35% & 49%
 of all students like
 multiple-choice exams.

Nov 14-8:03 AM

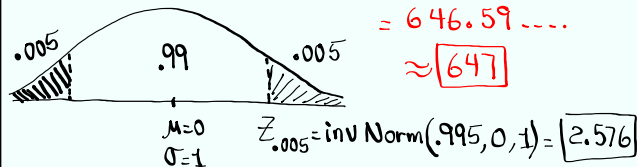
Suppose we like to construct 99% confidence interval for the prop. of all students in favor of multiple-choice exams and error not to exceed 5%, find min. Sample Size needed.

C-level: .99
 $E = .05$
 $\hat{p} = .42$

$$n = \hat{p} \hat{q} \left(\frac{Z_{\alpha/2}}{E} \right)^2$$

$$= (.42)(.58) \left(\frac{2.576}{.05} \right)^2$$

$$= 646.59 \dots \approx \boxed{647}$$



If $\hat{p}$ & $\hat{q}$ were unknown,

$$n = .25 \left(\frac{2.576}{.05} \right)^2 = 663.5776 \approx \boxed{664}$$

SG 21✓

Nov 14-8:14 AM

Estimating Population Mean μ :

SG 22

Final Ans: $\dots < \mu < \dots$

Format: $\bar{x} - E < \mu < \bar{x} + E$

$\uparrow$ Sample Mean
 Point-estimate

 $\uparrow$ Margin of error

Case I: σ known

C.V. $\rightarrow Z_{\alpha/2} \rightarrow \text{invNorm}$

Conf. Int $\rightarrow Z$ Interval

Inpt: Stats

Nov 14-8:23 AM

Given $n=32$, $\bar{x}=85$, $\sigma=12$

Find 90% Conf. interval for Pop. Mean μ

Since σ is known $\rightarrow$ use Z Interval

[STAT] $\rightarrow$ TESTS $\downarrow$ [ZInterval]

inpt: [Stats]

$$81.511 < \mu < 88.489$$

$$\sigma = 12$$

$$\bar{x} = 85$$

$$n = 32$$

$$C\text{-level: } .9$$

[Calculate]

Since $\bar{x}$ is a whole #,
we round to whole # as well.

$$82 < \mu < 88$$

we are 90% confident that
pop. means is between 82
and 88.

$$E = \frac{88 - 82}{2} = 3 \quad \bar{x} = \frac{88 + 82}{2} = 85$$

Nov 14-8:28 AM

I surveyed 35 students, their mean age was
32.5 yrs. $n=35$ $\bar{x}=32.5$

no C-level $\rightarrow .95$

Find Conf. interval for the mean age of all

students assuming standard deviation of ages
of all students was 7.5 yrs.

$$\sigma = 7.5$$

$$< \mu <$$

Since σ is known, we use

Z Interval

$$30.015 < \mu < 34.985$$

inpt: [STATS]

Since $\bar{x}$ was in 1-dec.,
we round to 1-dec.

$$\sigma = 7.5$$

$$\bar{x} = 32.5$$

$$n = 35$$

$$C\text{-level: } .95$$

[Calculate]

$$E = \frac{35 - 30}{2} = 2.5$$

$$\bar{x} = \frac{35 + 30}{2} = 32.5$$

$$30.0 < \mu < 35.0$$

Nov 14-8:35 AM

Estimating Population Mean μ :

SG 22

Final Ans: $\dots < \mu < \dots$

Format: $\bar{x} - E < \mu < \bar{x} + E$

$\uparrow$ Sample Mean
Point-estimate
 $\uparrow$ Margin of error

Case I: σ Known

Case II: σ unknown

C.V. $\rightarrow Z_{\alpha/2} \rightarrow \text{invNorm}$

C.V. $\rightarrow t_{\alpha/2} \rightarrow \text{invT}$

Conf. Int $\rightarrow Z\text{Interval}$

Conf. Int. $\rightarrow T\text{Interval}$

Inpt: Stats

inpt: Stats

df = n - 1

Nov 14-8:23 AM

Given $n=15$ $\bar{x}=48$ $S=10$

Find 98% Conf. interval for pop. mean μ .

Since σ is unknown $\rightarrow T\text{Interval}$

inpt: Stats

$41.224 < \mu < 54.776$

Since $\bar{x}$ is a whole #,

round to whole #,

$df=14 \leftarrow n=15$

$\bar{x}=48$

$S=10$

C-level: .98

$41 < \mu < 55$

Calculate

$$E = \frac{55 - 41}{2} = \boxed{7}$$

$$\bar{x} = \frac{55 + 41}{2} = \boxed{48}$$

Nov 14-8:47 AM

I surveyed 20 nurses, their mean monthly salary was \$6250 with standard dev. of \$275. $n=20$ $\bar{x}=6250$ $S=275$

No C-level $\rightarrow .95$

Find Conf. interval for the mean monthly salary of all nurses.

σ unknown $\rightarrow$ T Interval

inpt: **STATS**

$$6121 < \mu < 6379$$

$$\bar{x} = 6250$$

$$E = \frac{6379 - 6121}{2} = 129$$

$$S = 275$$

$$df = 20 - 1 = 19$$

$$n = 20$$

$$\bar{x} = \frac{6379 + 6121}{2} = 6250$$

$$C\text{-level}: .95$$

Calculate

Nov 14-8:53 AM

How to determine minimum Sample Size:

$$E = Z_{\alpha/2} \cdot \frac{\sigma}{\sqrt{n}}$$

use Algebra to Solve for n .

$$n = \left(\frac{Z_{\alpha/2} \cdot \sigma}{E} \right)^2 \quad \text{if decimal} \rightarrow \text{Round-up}$$

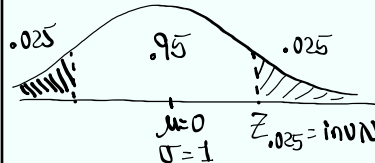
If σ is unknown, use S in place of σ .

$$n = \left(\frac{Z_{\alpha/2} \cdot S}{E} \right)^2$$

Nov 14-9:00 AM

Find min. Sample Size needed if we wish to construct 95% Conf. interval for Pop. mean when $\sigma=25$ and $E=8$.

$$n = \left(\frac{Z_{\alpha/2} \cdot \sigma}{E} \right)^2 = \left(\frac{1.960 \cdot 25}{8} \right)^2 = 37.515625 \approx \boxed{38}$$



Redo with $E=10$.

$$n = \left(\frac{1.960 \cdot 25}{10} \right)^2 = 24.01 \approx \boxed{25}$$

Redo with $E=4$

$$n = \left(\frac{1.960 \cdot 25}{4} \right)^2 = 150.0625 \approx \boxed{151}$$

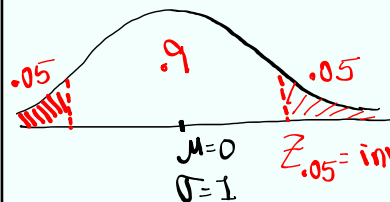
Nov 14-9:05 AM

Given $S=15$, $E=5$, C-level: .9

Find min. Sample Size needed to construct Conf. interval for pop. mean.

$$n = \left(\frac{Z_{\alpha/2} \cdot \sigma}{E} \right)^2 \quad \text{Since } \sigma \text{ is unknown}$$

$$n = \left(\frac{Z_{\alpha/2} \cdot S}{E} \right)^2 = \left(\frac{1.645 \cdot 15}{5} \right)^2 = 24.35 \dots \approx \boxed{25}$$



SG 22✓

Nov 14-9:14 AM